Appendix C

Kernels and Phase speeds

C.1 Scaling Kernels

Since it is numerically impossible to capture a delta function, we define the anomalies by the following sharply decaying functions,

$$\frac{\delta c^2}{c^2} = 0.1\left\{1 - \frac{1}{1+\exp[8.2(1-r)]}\right\}, \tag{C.1}$$

and

$$\frac{\delta a}{a} = -\left\{1 - \frac{1}{1+\exp[8.9(1-\tilde{r})]}\right\}, \tag{C.2}$$

where $r = \sqrt{x^2+y^2+z^2}$ has units of Mm, and $(0,0,0)$ is the center of the perturbation (it is vertically localized at the level of the photosphere). We use the notation of Gizon & Birch (2002) to describe a source perturbation in equation (C.2), where a is the strength of the unperturbed source and the deactivated source is located around the point (x_0, y_0, z_0), with $\tilde{r} = \sqrt{(x-x_0)^2 + (y-y_0)^2}$ (units of Mm also) and $z_0 = -200$ km. Since the f mode is the diagnostic agent in this case, we assume that the anomaly is essentially 2D in nature. To transform travel-time shifts to kernel magnitudes for the sound-speed perturbation case, consider the function from equation (C.1) applied to equation (3.7). Assuming the kernel varies much slower than the perturbation, we can rewrite equation (3.7) as:

$$\delta\tau_{\mathrm{mean/diff}}(\mathbf{r}) = K_{\mathrm{mean/diff}}(\mathbf{r}, 0; \Delta) \int\int\int_{\odot} \frac{\delta c^2}{c^2}(\mathbf{r}', z) d\mathbf{r}' dz, \tag{C.3}$$

which when integrated merely becomes the finite volume of the perturbation in equation (C.1). A similar 2D area integration ($z = -200$ km) is carried out for the source perturbation. Calculating these integrals, the kernel for the sound-speed perturbation (in units of $\mathrm{s/Mm^3}$) is

$$K_{\mathrm{mean/diff}}(\mathbf{r}, 0; \Delta) = 4.164\ \delta\tau_{\mathrm{mean/diff}}(\mathbf{r}), \tag{C.4}$$

and for the f-mode source kernel (in units of $\mathrm{s/Mm^2}$),

$$K_{\mathrm{mean/diff}}(\mathbf{r}, 0; \Delta) = -0.3056\ \delta\tau_{\mathrm{mean/diff}}(\mathbf{r}). \tag{C.5}$$

C.2 Phase Speeds

Eleven filters of mean phase-speed v and width δv are used for different ranges of annulus radii Δ, shown in Table C.1. The first column gives the annulus index, the last column gives the center t_0 of the window function used to measure first-bounce travel times (see text).

Table C.1. Annuli and Phase-Speed Filter Parameters

index	mean Δ (Mm)	Δ (Mm)	v (km s^{-1})	δv (km s^{-1})	t_0 (min)
1	6.20	03.7, 04.95, 06.20, 07.45, 08.7	16.40	2.63	19.00
2	8.70	06.2, 07.45, 08.70, 09.95, 11.2	19.28	2.63	19.17
3	11.60	08.7, 10.15, 11.60, 13.05, 14.5	22.26	2.63	20.00
4	16.95	14.5, 15.72, 16.95, 18.17, 19.4	27.24	3.68	25.00
5	24.35	19.4, 21.87, 24.35, 26.82, 29.3	35.73	3.94	27.50
6	30.55	26.0, 28.27, 30.55, 32.82, 35.1	40.06	3.94	29.17
7	36.75	31.8, 34.27, 36.75, 39.22, 41.7	43.25	3.94	30.83
8	42.95	38.4, 40.67, 42.95, 45.22, 47.5	49.20	3.94	33.33
9	49.15	44.2, 46.67, 49.15, 51.62, 54.1	55.80	4.46	35.00
10	55.35	50.8, 53.07, 55.35, 57.62, 59.9	59.25	4.46	36.67
11	61.65	56.6, 59.12, 61.65, 64.18, 66.7	64.37	4.46	38.33